

# Modelling of time dependencies in associations between health effects and protracted exposures

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Modelling associations between health effects and protracted exposures

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# Definitions

In biomedical research, an exposure event is frequently associated with a risk lasting for a defined period **in the future**

Similarly, the risk at a given time is commonly assumed as the results of protracted exposures experienced **in the past**

This phenomenon is common to environmental stressors, drugs, carcinogenic substances, amongst others

Proposed **statistical methods** depend on study design, type of data, research fields

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# A general modelling framework

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The main conceptual and analytical challenge is to model the (potentially complex) temporal pattern of risk due to time-varying exposures

The risk is modelled in terms of contributions depending on **intensity** and **timing** of multiple exposure events:  
⇒ **bi-dimensional** association

**Aim:** to develop a general conceptual and statistical framework to model this type of associations

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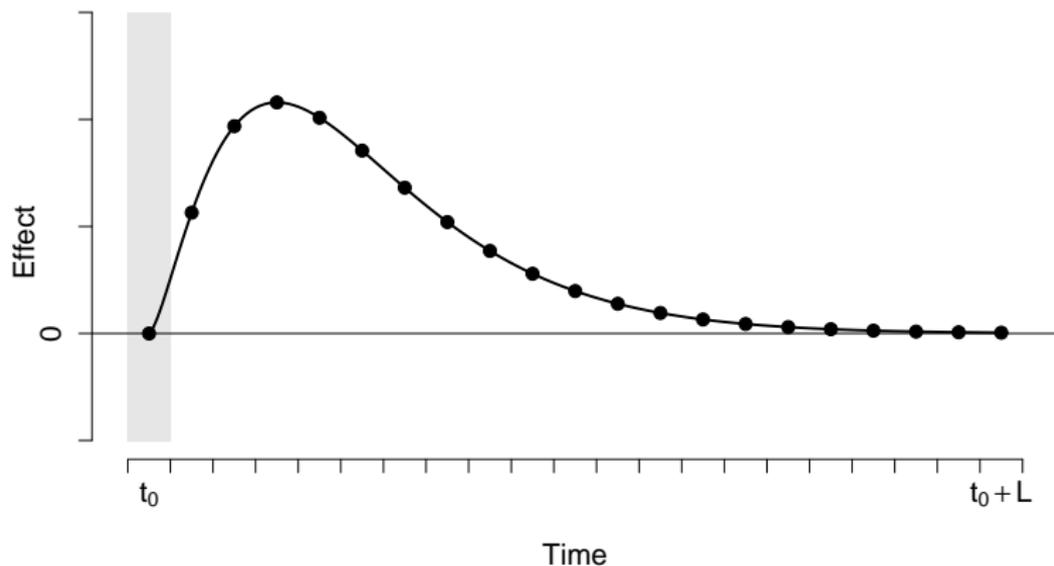
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# Conceptual representation

## Single exposure event



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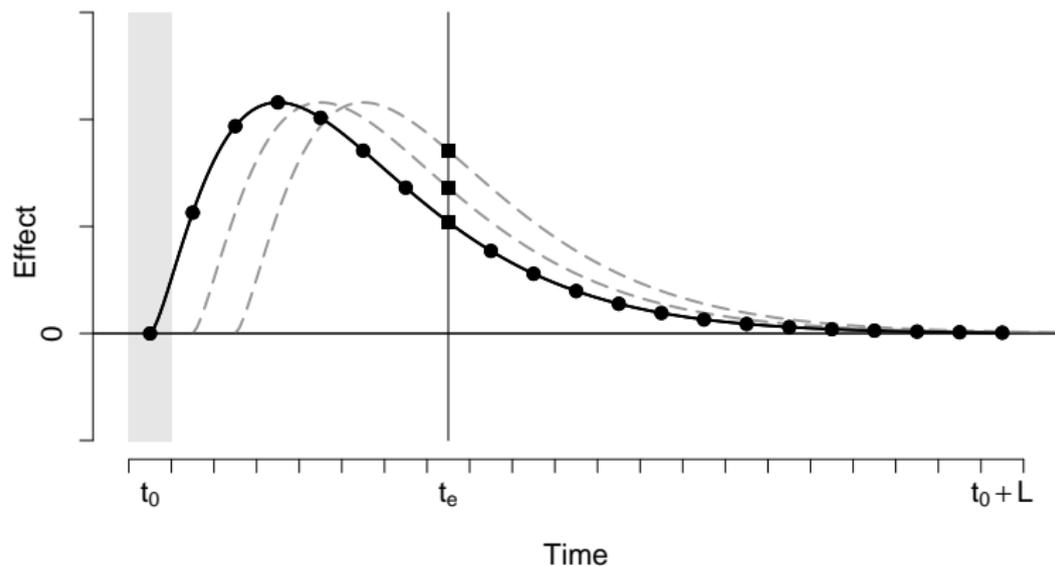
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# Conceptual representation

## Multiple exposure events



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# Perspectives and assumptions

Two perspectives:

- **forward**: from fixed exposure to future outcomes
- **backward**: from fixed outcome to past exposures

Additional assumptions:

- assumption of **independence**
- assumption of **identical** effects

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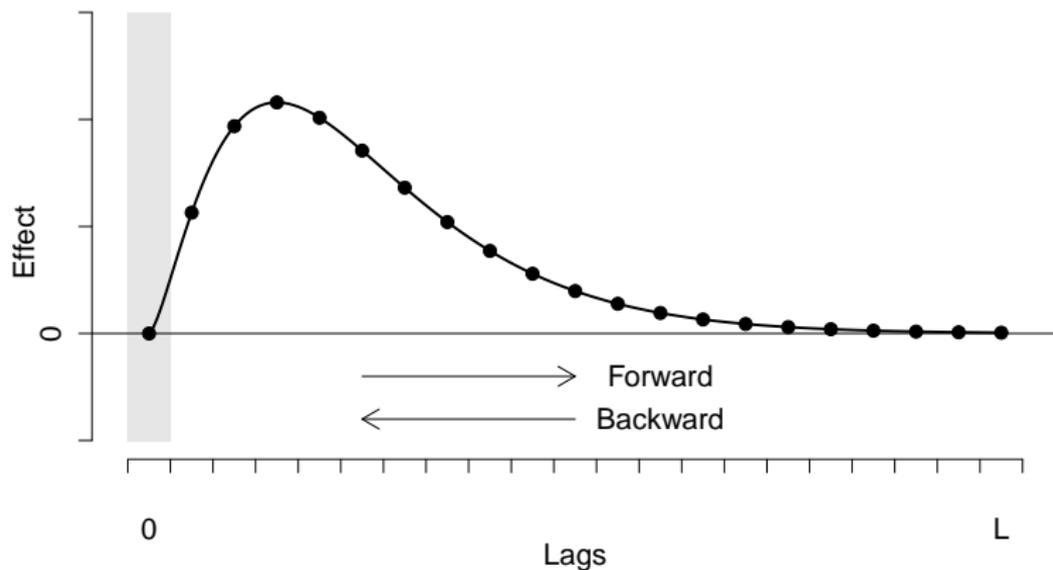
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# New lag dimension

## Lag or weighting curve



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# Approaches for cohort data

Simple **cumulative exposure** (Checkoway *AJIM* 1992)

**Exposure windows** (Langholz *AJIM* 1999)

Flexible approaches based on **weighting functions  $w$**   
(Thomas *SJWEH* 1983, Hauptmann *Biometrics* 2000, Richardson  
*Epidemiol* 2009, Sylvestre *Stat Med* 2009)

# Models with weighting function

A function  $s(x, t)$  for exposure-time response relationships:

$$s(x, t) = \beta_T \int_{t_0}^t w(t-u) x(u) du \approx \beta_T \sum_{u=t_0}^t w(t-u) x(u) \quad (1)$$

Re-parameterizing in terms of  $\ell$ :

$$s(x, t) = \beta_T \int_0^L w(\ell) x(t-\ell) d\ell \approx \beta_T \sum_{\ell=0}^L w(\ell) x(t-\ell) \quad (2)$$

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# Distributed lag models (DLMs)

Developed for time series data in econometrics (Almon *Econometrica* 1965), and recently extended to epidemiology (Schwartz *Epidemiology* 2000)

Based on the concept of **lag curve**, analogous to the weighting curve described above

These models can be extended **beyond** time series data

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# DLMs: algebra

First define the lag vector:

$$\ell = 0, \dots, \ell, \dots, L \quad (3)$$

and the vector  $\mathbf{q}$  of exposure histories:

$$\mathbf{q} = [x_t, \dots, x_{t-\ell}, \dots, x_{t-L}]^T \quad (4)$$

Then, given a basis matrix  $\mathbf{C}$  derived from  $\ell$ :

$$s(x, t; \boldsymbol{\eta}) = \mathbf{q}^T \mathbf{C} \boldsymbol{\eta} = \mathbf{w}^T \boldsymbol{\eta} \quad (5)$$

# DLMs: interpretation

The **lag-basis** function:

$$s(x, t; \boldsymbol{\eta}) = \mathbf{q}^T \mathbf{C} \boldsymbol{\eta} = \mathbf{w}^T \boldsymbol{\eta} \quad (6)$$

with  $\hat{\boldsymbol{\beta}} = \mathbf{C} \hat{\boldsymbol{\eta}}$  as **weights** defining the lag curve

**Q** is the matrix of exposure histories, **W** the matrix of transformed variables

Different DLMs with **alternative options** for the basis to compute **C** (step, splines, etc.)

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# The CPUM cohort

**3,347 subjects** working in the Colorado Plateau mines between 1950–1960

Vital status and cause of death collected through record linkage up to 1982, with **258 lung cancer deaths**

Exposure history to **radon** (WLM) and **tobacco smoke** (pack $\times$ 100) reported for 5-years age periods

# Modelling strategy

Association between radon and mortality for lung cancer

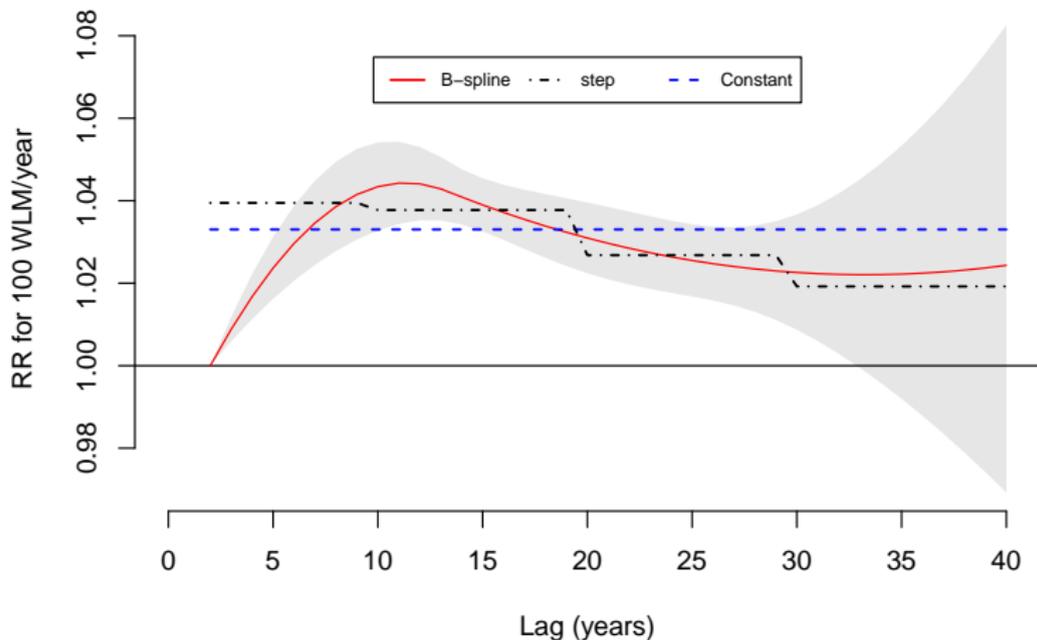
Analysis with Cox proportional hazards model for **time-varying exposures**

Age as time axis, controlling for smoking and calendar year

Exposure histories in WLM/year reconstructed for each of the **subject/periods** withing a **lag period 2–40**

**Different functions** used to estimate the lag curve:  
constant, step constant, quadratic B-spline

# Lag curves for DLMs



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**Table:** DLMs with different functions for  $\ell$ .

<i>Function for <math>x</math></i>	<i>Function for <math>\ell</math></i>	<i>df</i>	<i>AIC</i>
Linear	Constant	1	2581.5
Linear	Step function <sup>a</sup>	4	2582.7
Linear	B-spline <sup>b</sup>	3	2583.2

<sup>a</sup> Cut-offs at lag 10-20-30

<sup>b</sup> Quadratic, 1 knot at lag 13.3, no intercept

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# Non-linear extension: DLNMs

Main limitation: assumption of a linear exposure-response dependency

DLMs can be extended as well to non-linear relationships, leading to **distributed lag non-linear models (DLNMs)** (Armstrong *Epidemiology* 2006, Gasparrini *Stat Med* 2010)

Link with previous work on the extension to non-linear dependencies (Abrahamowicz *Stat Med* 2007, Berhane *Stat Med* 2008)

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# DLNMs: algebra

Another function for modelling non-linearity applied to  $\mathbf{q}$  in (4), deriving the basis matrix  $\mathbf{R}$ . A DLNM is based on the **cross-basis** function:

$$s(x, t; \boldsymbol{\eta}) = \sum_{j=1}^{v_x} \sum_{k=1}^{v_\ell} \mathbf{r}_{.j}^T \mathbf{c}_{.k} \eta_{jk} = \mathbf{w}^T \boldsymbol{\eta} \quad (7)$$

Algebra is intricate, but concept is straightforward: applying 2 different functions to model a **bi-dimensional** association

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# Extended results

**Table:** DLNMs with different functions for  $\ell$  and  $x$ .

<i>Function for <math>x</math></i>	<i>Function for <math>\ell</math></i>	<i>df</i>	<i>AIC</i>
Linear	Constant	1	2581.5
Linear	Step function <sup>a</sup>	4	2582.7
Linear	B-spline <sup>b</sup>	3	2583.2
B-spline <sup>c</sup>	Constant	3	2528.0
Step function <sup>d</sup>	Step function <sup>a</sup>	8	2507.0
B-spline <sup>c</sup>	B-spline <sup>b</sup>	9	2500.1

<sup>a</sup> Cut-offs at lag 10-20-30

<sup>b</sup> Quadratic, 1 knot at lag 13.3, no intercept

<sup>c</sup> Quadratic, 1 knot at 59.4 WLM/year, no intercept

<sup>d</sup> Cut-offs at 26-121 WLM

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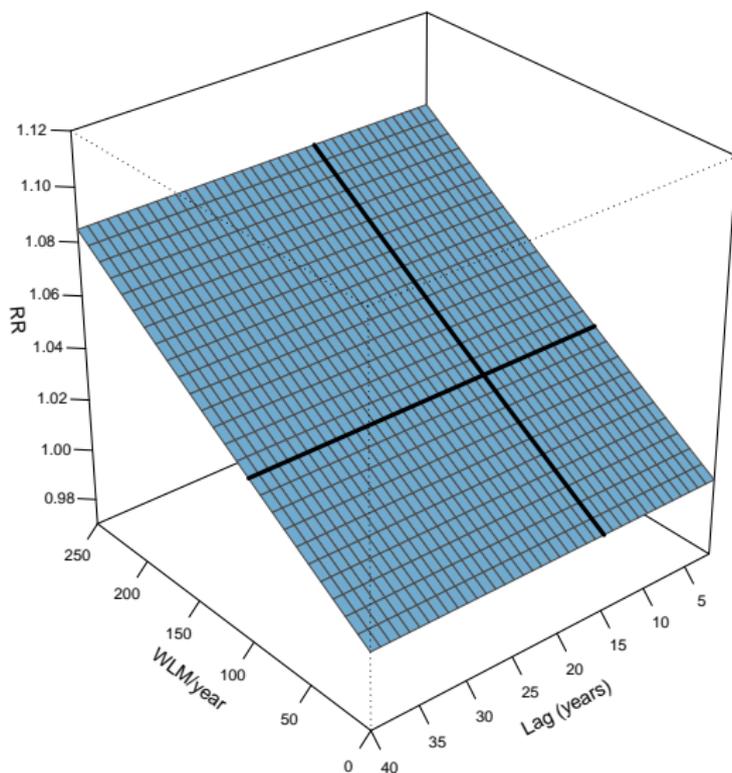
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# 3D: linear-by-constant



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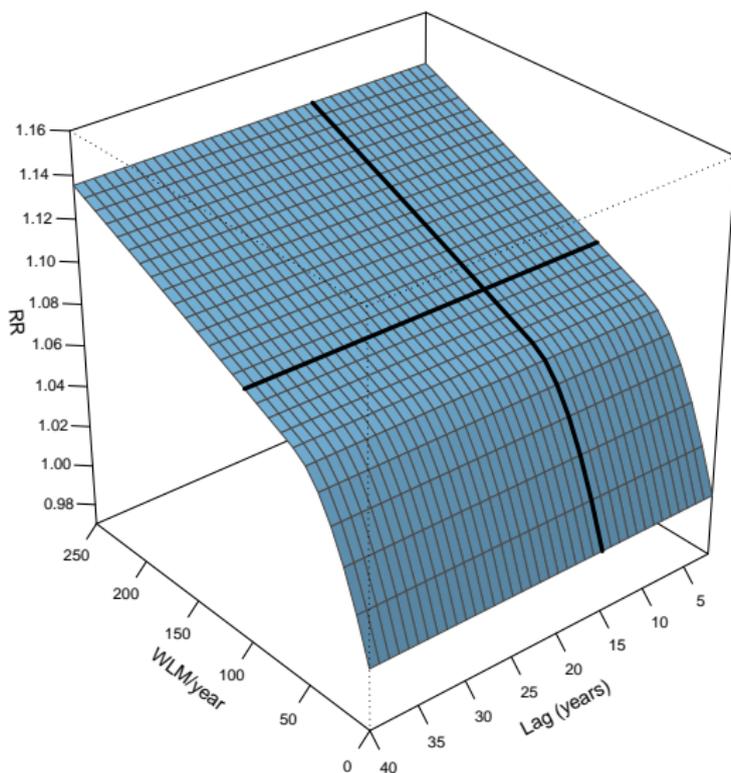
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# 3D: spline-by-constant



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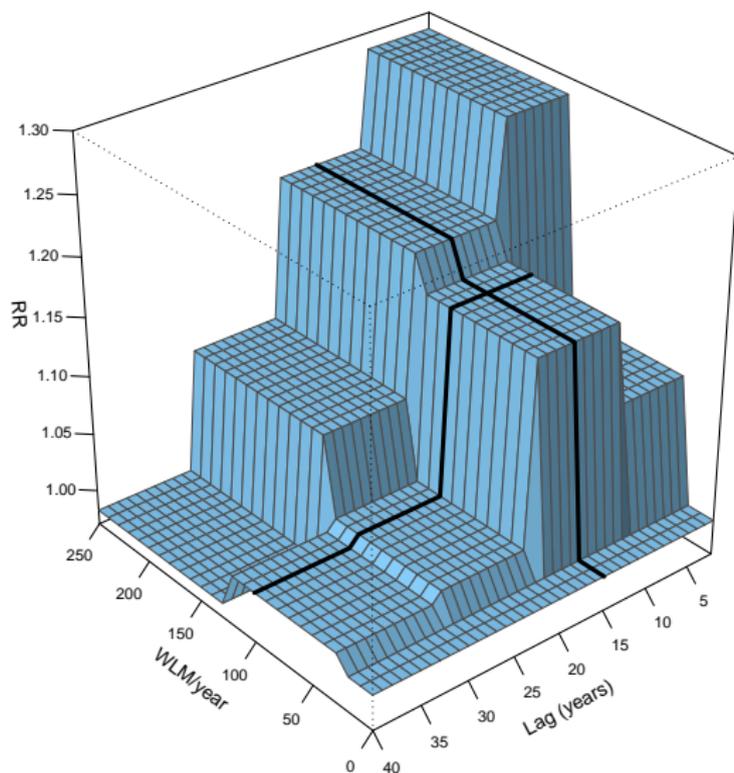
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# 3D: step-by-step



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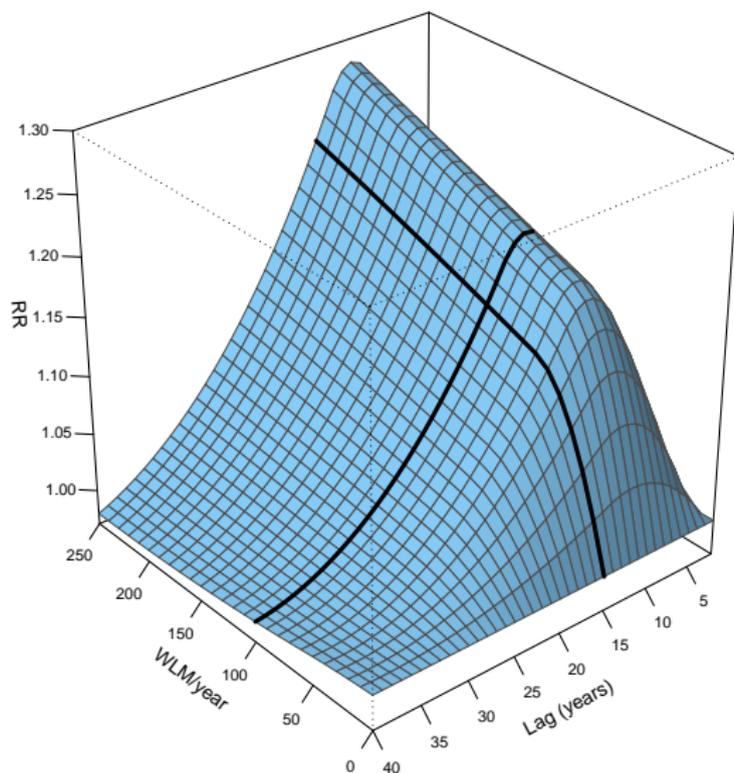
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# 3D: spline-by-spline



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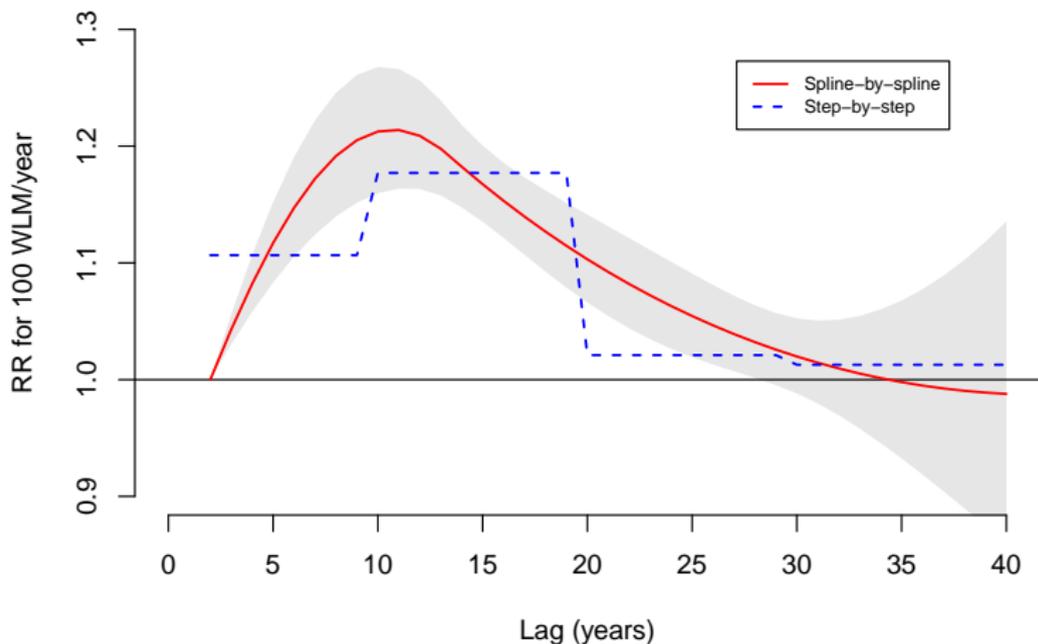
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# Lag curves: comparison



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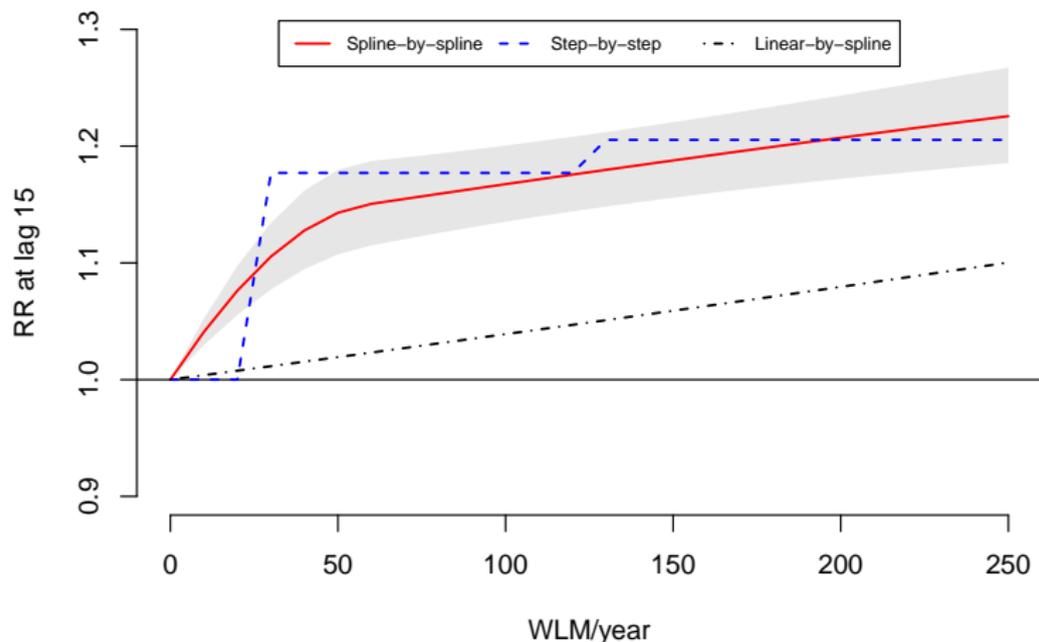
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# Exposure-response: comparison



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# Predicted risk: 20 WLM for 10yrs

**Table:** Predicted risk from different models.

<i>Model</i>	<i>RR</i>
Linear-by-constant	1.053 (1.045–1.062)
Linear-by-spline	1.039 (1.027–1.050)
Spline-by-constant	1.361 (1.245–1.487)
Spline-by-spline	1.550 (1.331–1.805)

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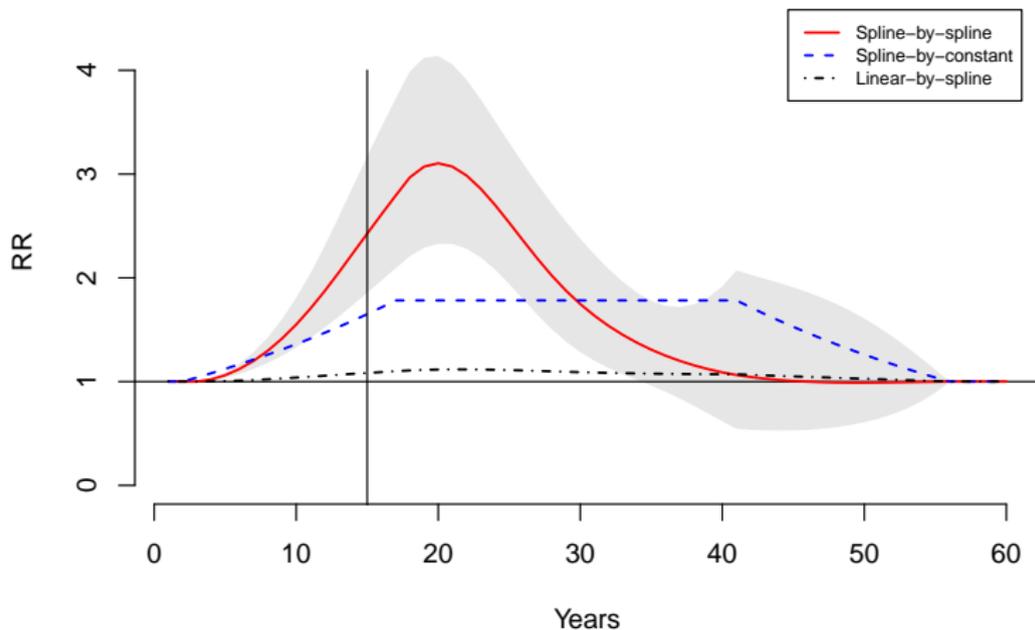
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# Evolution of risk: 20WLM for 15yrs



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# A unified framework

DLNMs offer a flexible way to model **complex time dependencies** in associations with protracted exposures

Potentially applicable in different setting (study design, data structure) where the risk is assumed to be associated with **protracted time-varying** exposures

The framework is based on a **simple conceptual scheme** which provides basis for interpretation and defines assumptions

# Statistical and computational advantages

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**Statistical** and **theoretical** development of DLNMs  
available in this extended framework

Based on entirely parametric approaches, with CI and tests  
off the shelf

Models can be fitted with **standard regression routines**

The framework is **fully implemented** in the R package  
`dlnm`, available from the CRAN (Gasparri *JSS* 2011)

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# The R package dlnm

## Example of code

```
library(dlnm)

cb <- crossbasis(Q,lag=c(2,40),
  argvar=list(type="bs",degree=2,knots=59.4,cen=0),
  arglag=list(type="bs",degree=2,knots=13.3,int=F))

model <- coxph(Surv(agest,ageexit,ind)~cb+smoke+caltime,data)

pred <- crosspred(cb,model11,at=0:25*10)

plot(pred,"3d",xlab="WLM/year",ylab="Lag (years)",zlab="RR")
plot(pred,var=100,xlab="Lag (years)",ylab="RR")
plot(pred,lag=15,xlab="WLM/years",ylab="RR")
```

# Limitations

The main requirement is the availability of (possibly reconstructed) **exposure histories** for each observation (subject)

Exposure histories need to show **variability** between and within observations

More complex DLNMs need a relatively high statistical power

**Model selection** issues

# Applications

- **Time series:** association between air pollution/temperature and mortality/morbidity – analysis in several cities/countries
- **Matched case-control:** association between gestational exposure to pesticides and autism – a study in California
- **Life course cohort:** association between body size during infancy/childhood and hip dysplasia at skeletal maturity – Bergen Hip Cohort Study

# Potential applications

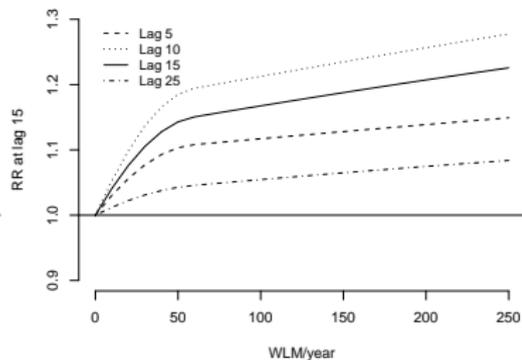
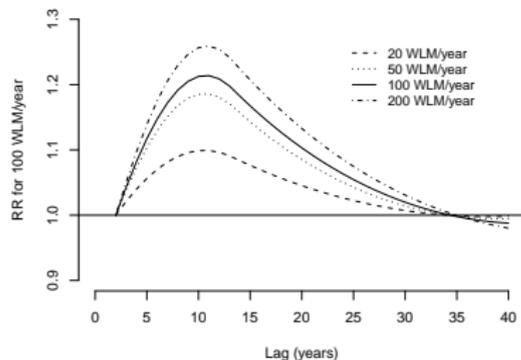
- Analysis of other occupational cohorts
- Association between smoking and lung cancer/cardiovascular risk
- Life course studies (Framingham Heart Study)
- ....

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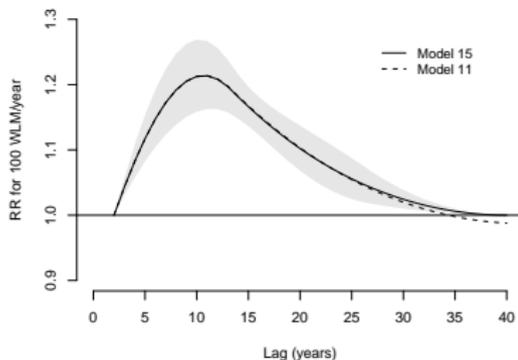
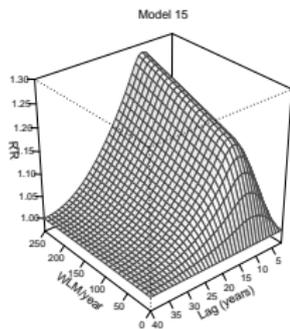
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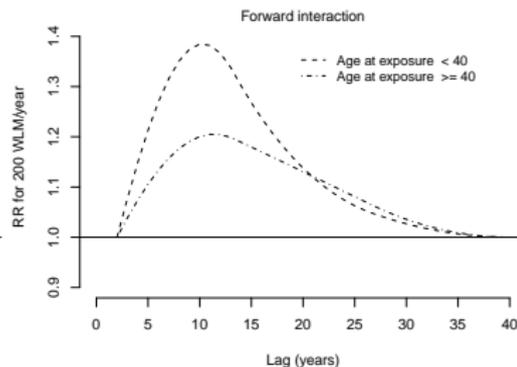
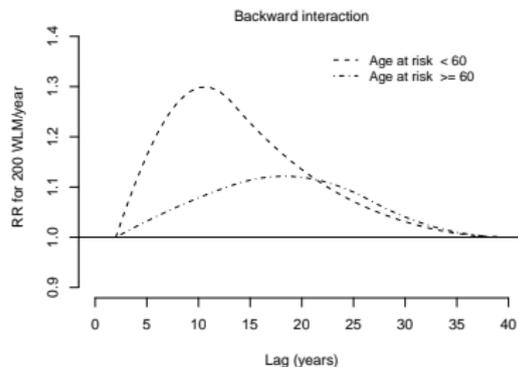
References

Additional slides

# Interaction

Modelling  
associations  
between health  
effects and  
protracted  
exposures

Gasparrini A



The issue

Conceptual  
framework

Statistical  
development

Cohort  
DLMs

An example

Data & models  
Results

Extension

DLNMs  
Extended results  
Predictions

Comments

References

Additional slides